

Operational Ocean analysis from Ocean data assimilation Systems

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With inputs from:

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Numerical Models

Hindcasting

Nowcasting

Forecasting

Past

Present

Future

Data Assimilation= Model + Observations

Re-Analysis

Analysis

Past

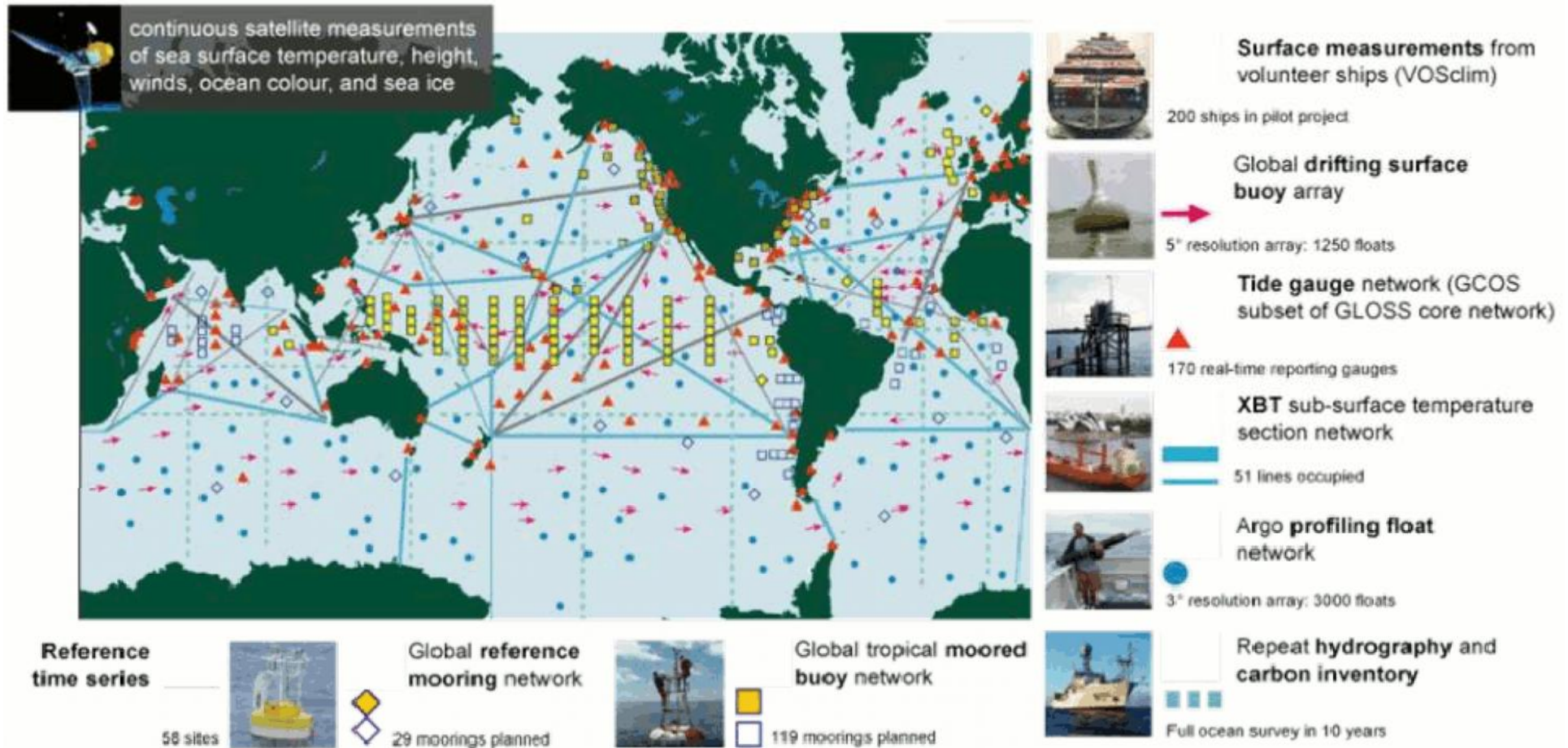
Present



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Ocean Observation Networks



- A total of 5635 platforms are maintained globally.

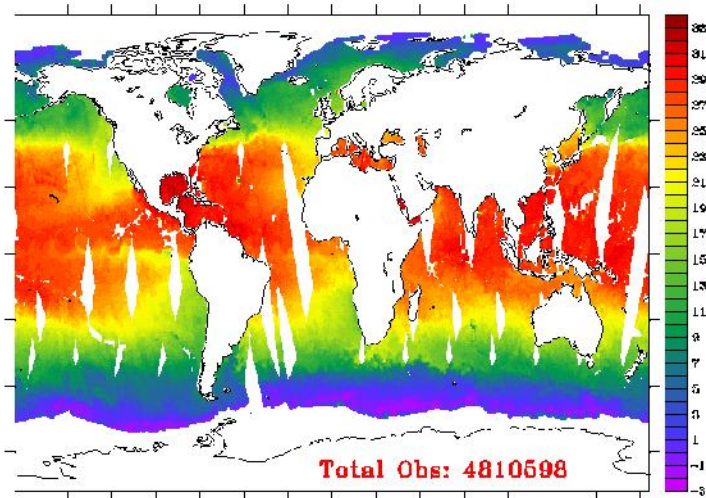


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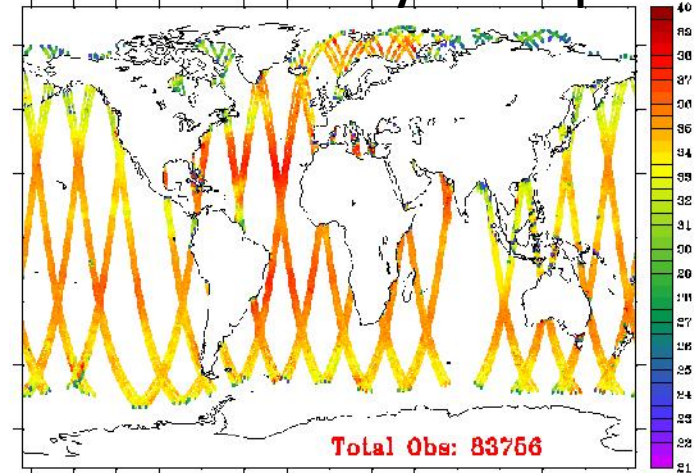


Spatial Coverage from different satellites for different parameters (25th August, 2011)

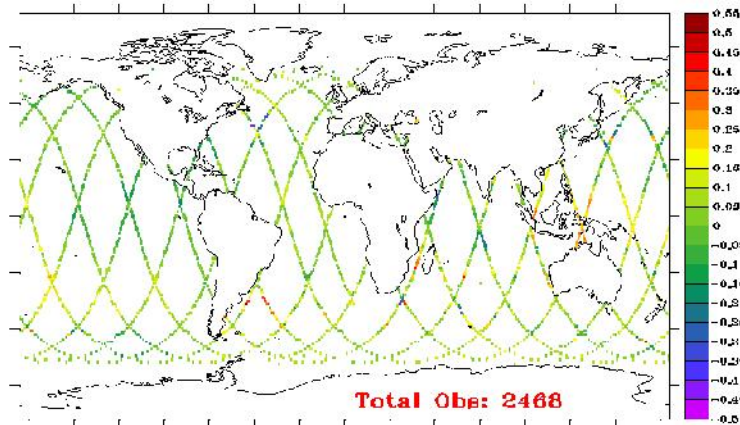
Sea Surface Temperature from AMSRE



Sea Surface Salinity from Aquarius



Sea Surface Height Anomaly from Altimeters

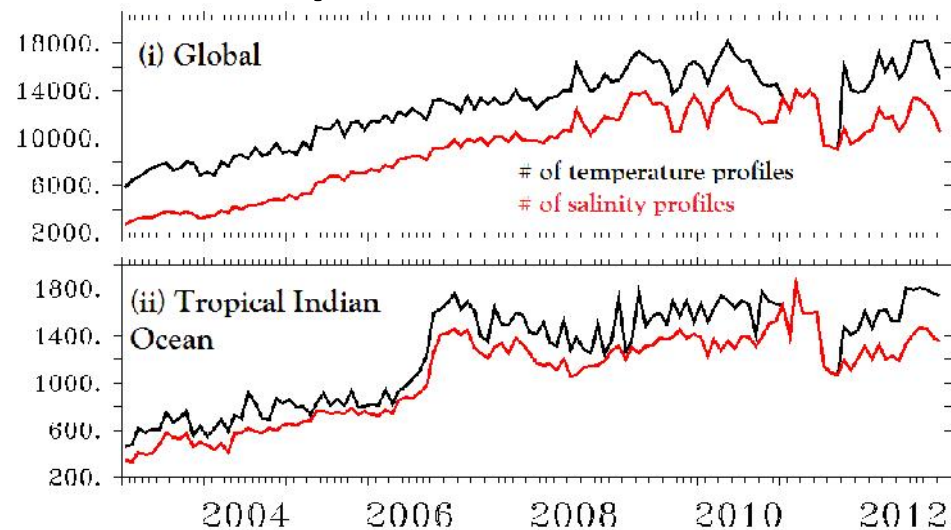
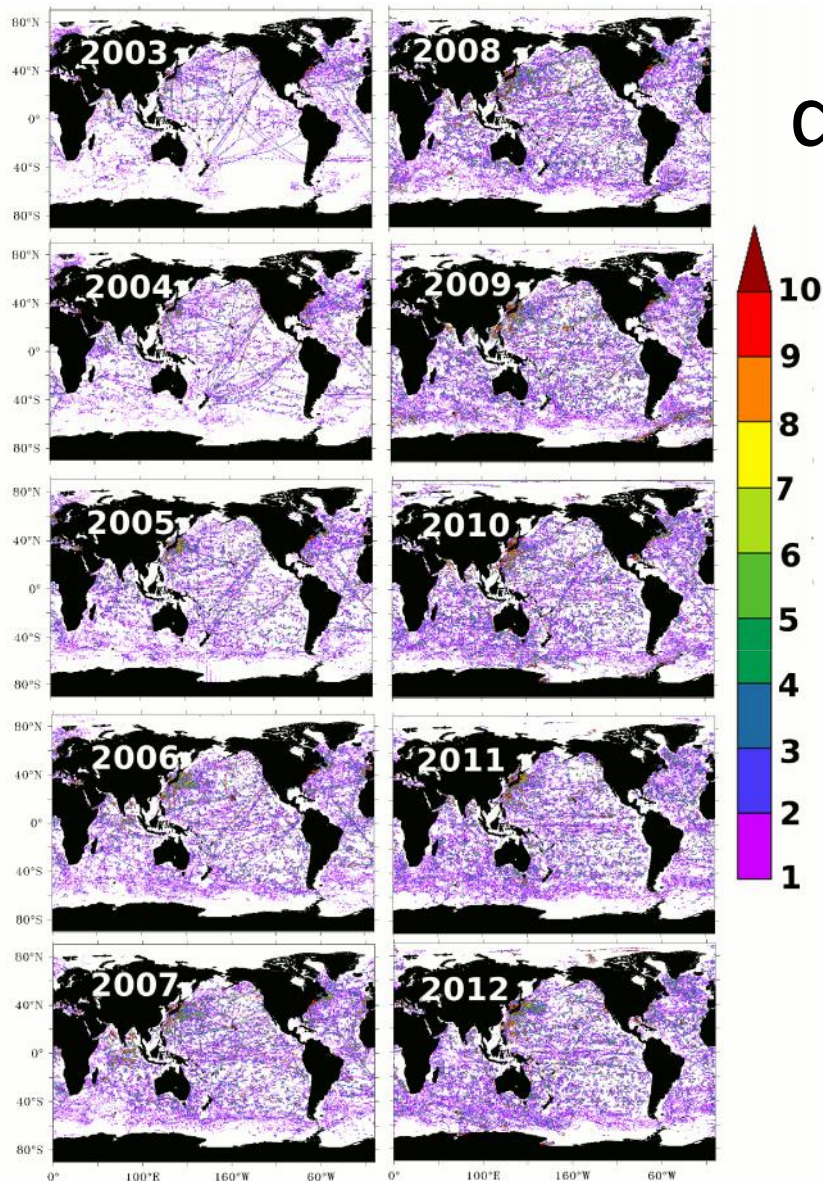


Limitation:

Cannot provide sub-surface information



Spatial coverage from different in-situ observation networks for ocean T&S profiles



Limitations:

Impossible to observe the ocean at each and every time and location.

Most of the ocean is largely under-sampled even today.



Numerical Ocean Models

Primitive Equations for ocean:

$$x\text{-momentum} \quad \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} = -\frac{1}{\rho_0} \frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left(A \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial z} \left(V_E \frac{\partial u}{\partial z} \right) \quad (1.1)$$

$$\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} = -\frac{1}{\rho_0} \frac{\partial p}{\partial y} - f u + \frac{\partial}{\partial x} \left(A \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial y} \left(A \frac{\partial v}{\partial y} \right) + \frac{\partial}{\partial z} \left(V_E \frac{\partial v}{\partial z} \right) \quad (1.2)$$

$$z\text{-momentum} \quad \frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial z} - g \quad (1.3)$$

$$\frac{\partial}{\partial t} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + q_w \quad (1.4)$$

$$\text{Tracer (Temperature)} \quad \frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} = \frac{\partial}{\partial x} \left(K \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left(K \frac{\partial T}{\partial y} \right) + \frac{\partial}{\partial z} \left(K \frac{\partial T}{\partial z} \right) + Q$$

$$\text{Equation of state: } \rho = \rho(\theta, S, p) \quad (1.6)$$

Discretizations

Unknown processes

Inputs at boundaries

Parameterizations

Important Approximations:

Boussinesq
Hydrostatic
Shallow-Ocean

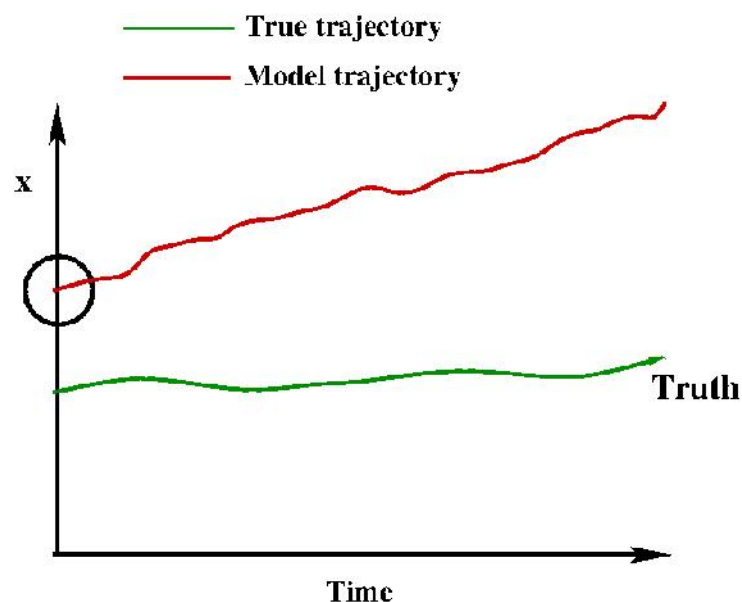
Limitations:

Inability to model all the ocean process.
Model errors aroused due to various approximations/discretizations

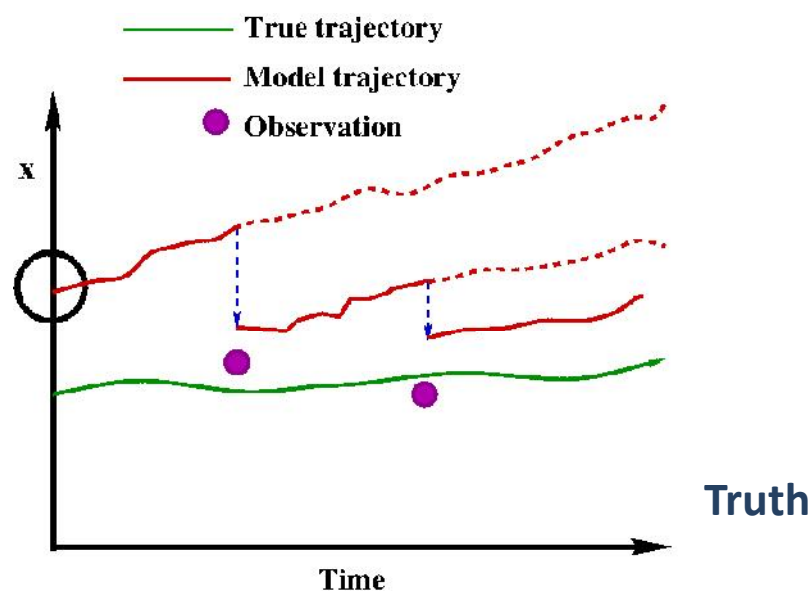


Flowchart of Data Assimilation

Definition: Data assimilation is an analysis technique in which the observed information is accumulated into the model state by taking advantage of consistency constraints with laws of time evolution and physical properties



NO CORRECTION



CORRECTION

Application: Improved solutions of the state of the ocean realized from both model and observations (temperature, salinity, SLA, and currents).



$$X^a = x^b + BH^T (HBH^T + R)^{-1} (Y_o - Hx^b)$$

X^a --> *Analysis*

X^b --> *Forecast / Background*

Y_o --> *Observation*

B → Model background error covariance

R → Observational error covariance

H → Interpolation operator

What is the relative role of B and R

It is best understood if we work with a scalar case with $H=1$

$$\begin{aligned} \text{Let, } R &= \tau_o^2, B = \tau_b^2 \\ x^a &= x^b + \tau_b^2 (\tau_b^2 + \tau_o^2)^{-1} (y_o - x^b) \\ \Rightarrow x^a &= \frac{\tau_o^2}{\tau_o^2 + \tau_b^2} x^b + \frac{\tau_b^2}{\tau_o^2 + \tau_b^2} y_o \end{aligned}$$

Analysis is sensitive to both model background error covariance and observational error covariance

If $\tau_b \gg \tau_o$

$x^a \approx y_o$

If $\tau_o \gg \tau_b$

$x^a \approx x_b$



$$X^a = X^b + BH^T (HBH^T + R)^{-1} (Y_o - HX^b)$$

What is the role of B ??

X^a --> Analysis

X^b --> Forecast / Background

Y_o --> Observations

B --> Model background error covariance

R --> Observational error covariance

H --> Interpolation operator

7

8

9

4

5

6

1

2

3

obs

Under what condition will the information at grid location 3 propagate to other grid points ?



$$x^a = x^b + BH^T (HBH^T + R)^{-1} (y - Hx^b)$$

$$x^b = \begin{bmatrix} x_1^b \\ x_2^b \\ \cdot \\ x_9^b \end{bmatrix}, \quad y = y_0, \quad H = [0 \quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0]$$

$$R = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \quad B = \begin{bmatrix} B_{11} & B_{12} & \cdot & \cdot & \cdot & B_{19} \\ B_{21} & B_{22} & \cdot & \cdot & \cdot & B_{29} \\ \cdot & \cdot & B_{33} & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ B_{31} & B_{32} & \cdot & \cdot & \cdot & B_{39} \end{bmatrix}$$

$$y - Hx^b = y_0 - [0 \quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0] \begin{bmatrix} x_1^b \\ x_2^b \\ \cdot \\ x_9^b \end{bmatrix} = y_0 - x_3^b$$



$$x^a = x^b + BH^T (HBH^T + R)^{-1} (y - Hx^b)$$

$$HB = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} B_{11} & B_{12} & \cdot & \cdot & \cdot & B_{19} \\ B_{21} & B_{22} & \cdot & \cdot & \cdot & B_{29} \\ \cdot & \cdot & B_{33} & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ B_{31} & B_{32} & \cdot & \cdot & \cdot & B_{39} \end{bmatrix} = \begin{bmatrix} B_{31} & B_{32} & \cdot & \cdot & B_{39} \end{bmatrix}$$

$$HBH^T = \begin{bmatrix} B_{31} & B_{32} & \cdot & \cdot & B_{39} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \\ \cdot \\ 0 \end{bmatrix} = B_{33}$$

$$(HBH^T + R)^{-1} = \frac{1}{B_{33} + \dagger_0^2} \Rightarrow (HBH^T + R)^{-1} (y - Hx^b) = \frac{y_0 - x_3^b}{B_{33} + \dagger_0^2}$$



$$x^a = x^b + BH^T (HBH^T + R)^{-1} (y - Hx^b)$$

$$(HBH^T + R)^{-1} (y - Hx^b) = \frac{y_0 - x_3^b}{B_{33} + \sigma_0^2}$$

$$BH^T = \begin{bmatrix} B_{11} & B_{12} & \cdot & \cdot & \cdot & B_{19} \\ B_{21} & B_{22} & \cdot & \cdot & \cdot & B_{29} \\ \cdot & \cdot & B_{33} & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ B_{31} & B_{32} & \cdot & \cdot & \cdot & B_{39} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \\ \cdot \\ \cdot \\ 0 \end{bmatrix} = \begin{bmatrix} B_{13} \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ B_{93} \end{bmatrix}$$

$$BH^T (HBH^T + R)^{-1} (y - Hx^b) = \begin{bmatrix} B_{13} \\ \cdot \\ \cdot \\ \cdot \\ B_{93} \end{bmatrix} \frac{(y_0 - x_3^b)}{(B_{33} + \sigma_0^2)}$$



$$\begin{bmatrix} x_1^a \\ x_2^a \\ \cdot \\ \cdot \\ x_9^a \end{bmatrix} = \begin{bmatrix} x_1^b \\ x_2^b \\ \cdot \\ \cdot \\ x_9^b \end{bmatrix} + \begin{bmatrix} B_{13} \\ B_{23} \\ \cdot \\ \cdot \\ B_{93} \end{bmatrix} \frac{(y_0 - x_3^b)}{(B_{33} + \dagger^2_0)}$$

$$x_k^a = x_k^b + \left(\frac{y_0 - x_3^b}{B_{33} + \dagger^2_0} \right) B_{k3}$$

B propagates information from one site to another !!!



Data Assimilation Techniques

Nudging:

Simply adds a correction term to the prognostic equation of interest (example: SST equation)

$$\frac{\partial X}{\partial t} = K(X_o - X)$$

Limitation: Observation should exactly be on the model space.

Optimal Interpolation:

Gets correction at each grid point separately based on model and observational error covariance. The technique depends largely on the de-correlation lengths. Model error covariance is

$$X^a = X^b + BH^T (HBH^T + R)^{-1} (Y_o - HX^b)$$

Limitation: Corrections at a grid point is independent from other grid point which can lead to discontinuities in the solution. There is absolutely no scope for correction if there are no observations within the de-correlation length scales.



Data Assimilation Techniques

Variational Methods (3D-VAR and 4D-VAR):

Gets correction at each grid point based on a cost function that connects for the whole domain. The technique ensures smoothness in the solutions.

$$3D-VAR: J(X) = \frac{1}{2}(X - X^b)^T B^{-1}(X - X^b) + \frac{1}{2}(HX - Y_o)^T R^{-1}(HX - Y_o)$$

$$4D-VAR: J(X) = \frac{1}{2}(X - X^b)^T B^{-1}(X - X^b) + \frac{1}{2} \sum_{i=1}^n (HX - Y_o^i)^T R^{-1}(HX - Y_o^i)$$

Limitation: Model error covariance is static. In reality, they change with time and state of the ocean.

Kalman Filters :

Model error covariance that is required to obtain correction evolves with the model.

$$X^a = X^b + P^a H^T R^{-1} (Y_o - HX^b)$$
$$P^a = [I + P^b H^T R^{-1} H]^{-1} P^b$$

Limitations: Pure Kalman filters can not be applied to ocean systems. Ensemble methods that use the flavour of Kalman filters are popular in literature. They largely depends on initial ensemble and inflation parameter that is unphysical.

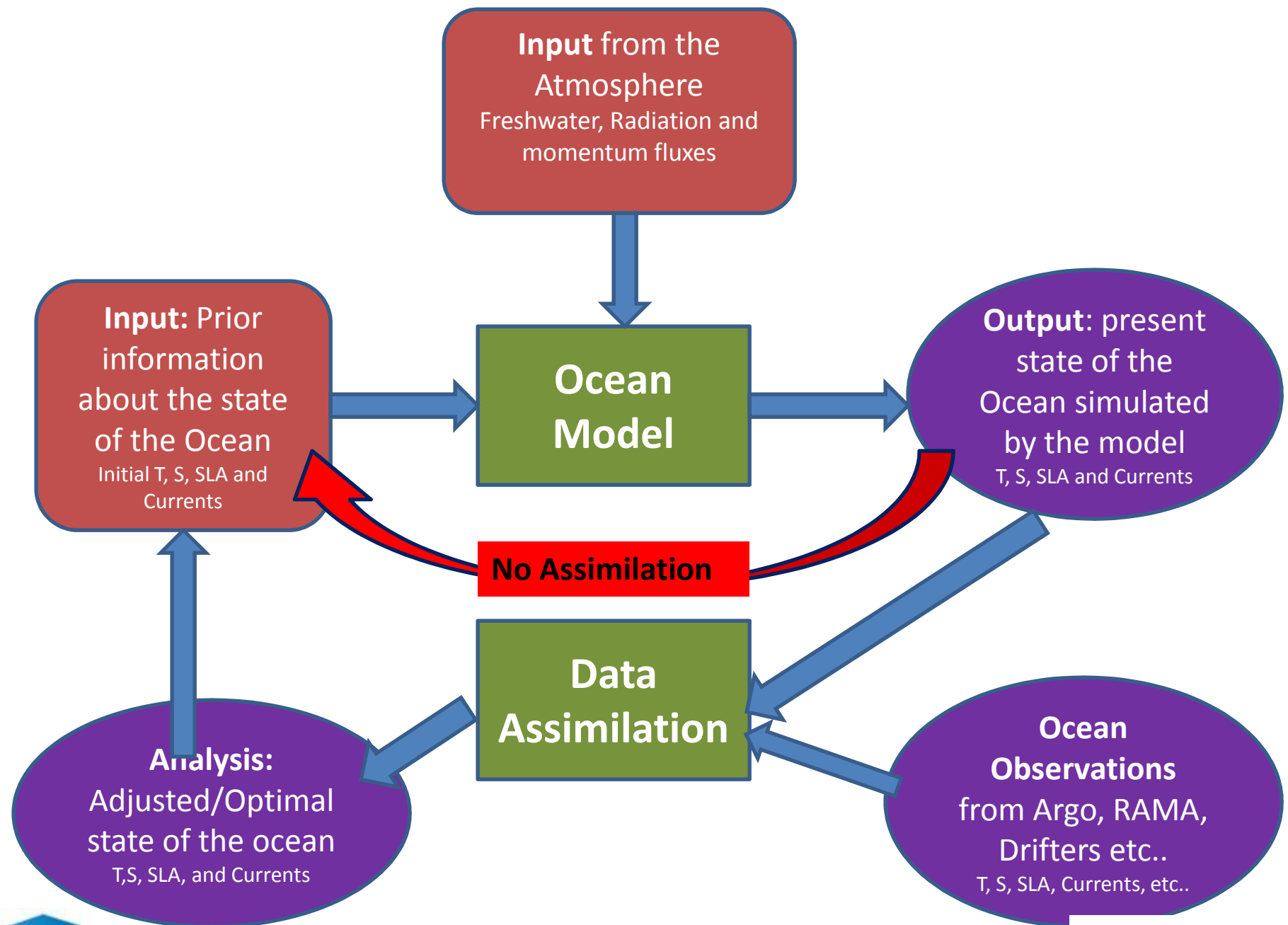


Limitations of Assimilation Schemes

Difficulty in prescribing the behavior of model errors, observational errors (instrument + representation)

Doesn't implicitly conform with the model dynamics. It can lead to dynamically inconsistent ocean states





Ocean Data Assimilation systems At INCOIS

	INCOIS-GODAS	LETKF-NEMO	LETKF-MOM	LETKF-ROMS
OGCM	MOM-4.0	NEMO	MOM-4.1	ROMS-3.6
Assimilation Scheme	3D-VAR	LETKF	LETKF	LETKF
Domain	Global	Global	Global	Indian Ocean
Assimilation capabilities	T&S profiles	SLA and T&S profiles	SST, SSS, SLA and T&S profiles	SST, SSS, SLA and T&S profiles
Status	Operational	Toy Model	Experimental	Experimental
Original source	Adopted from NCEP	Adopted from University of Maryland	Joint efforts between University of Maryland and INCOIS	Indigenous development
Reference	Ravichandran et al., 2013 Sivareddy, 2015	Sluka et al., 2016	--	--

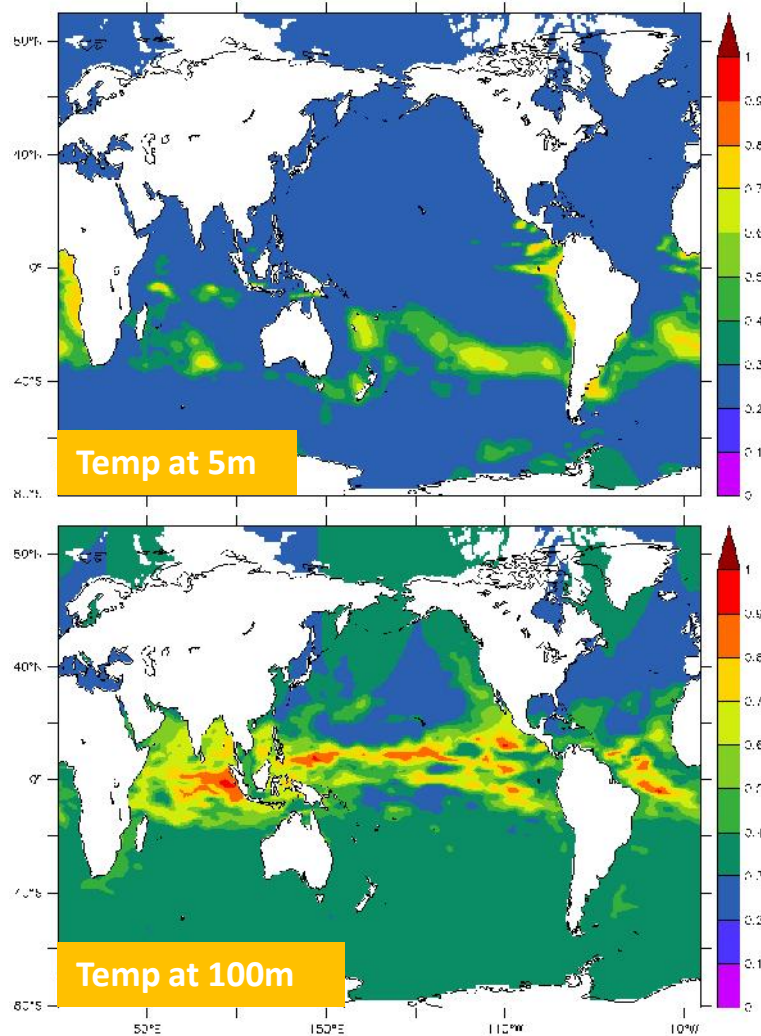


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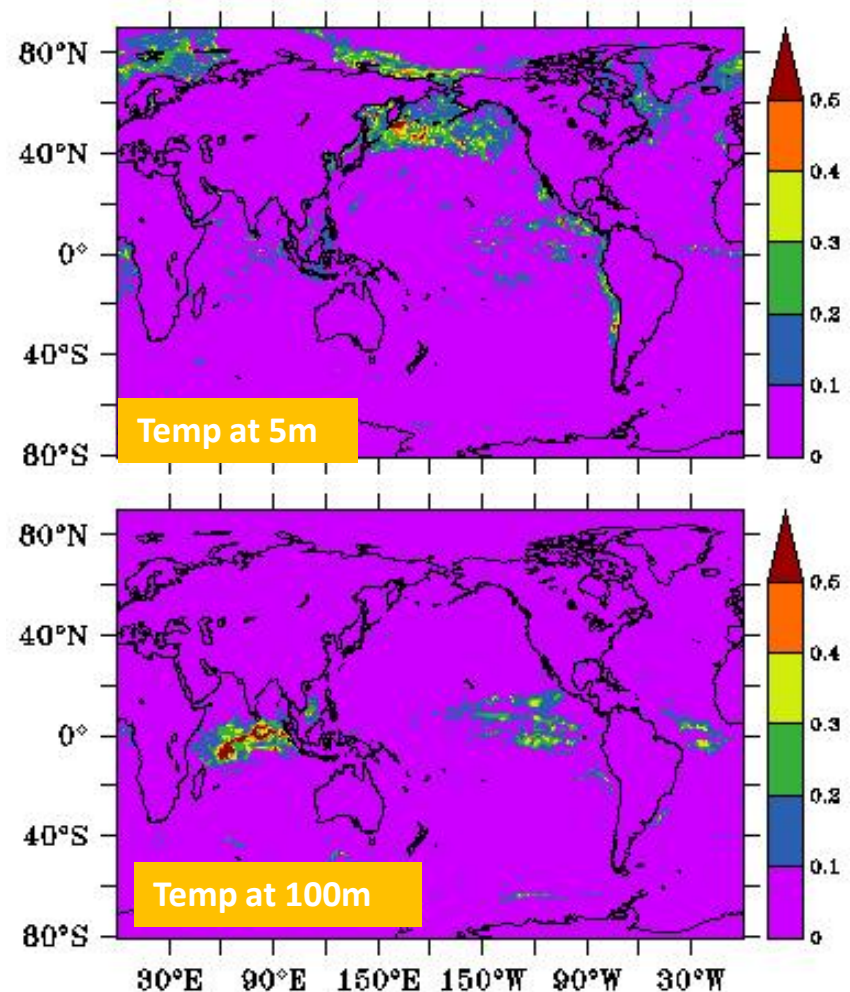


Model Errors set in INCOIS-GODAS and LETKF-MOM

INCOIS-GODAS



LETKF-MOM

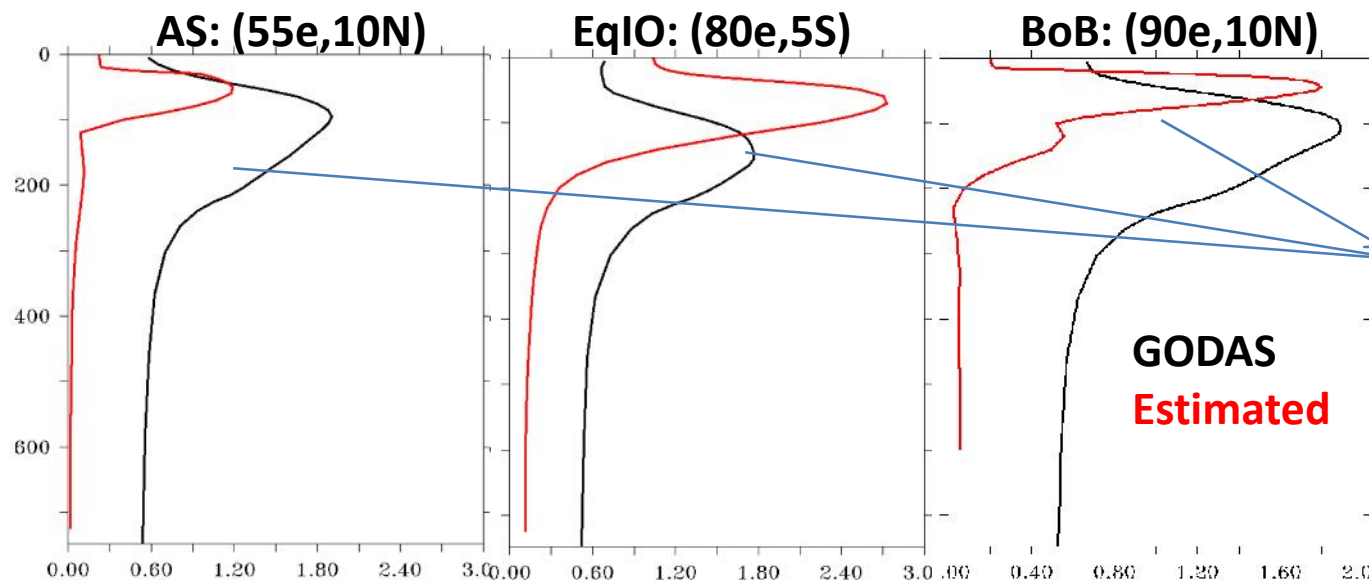


Observational Errors from high resolution simulations

In INCOIS-GODAS, Observational error is estimated based on local vertical gradient (e.g. local vertical temperature gradient)

In LETKF-MOM and LETKF-ROMS **observational error is estimated based on high resolution outputs from ROMS**

$$OE = \frac{1}{(\Delta i \times \Delta j)} \sum_{ii=i, jj=j}^{ii=i+\Delta i, jj=j+\Delta j} \left(H \overline{X}_{ii, jj} - X_{ii, jj} \right)^2 \quad \overline{X} = \frac{1}{(\Delta i \times \Delta j)} \sum_{ii=i, jj=j}^{ii=i+\Delta i, jj=j+\Delta j} X_{ii, jj}$$

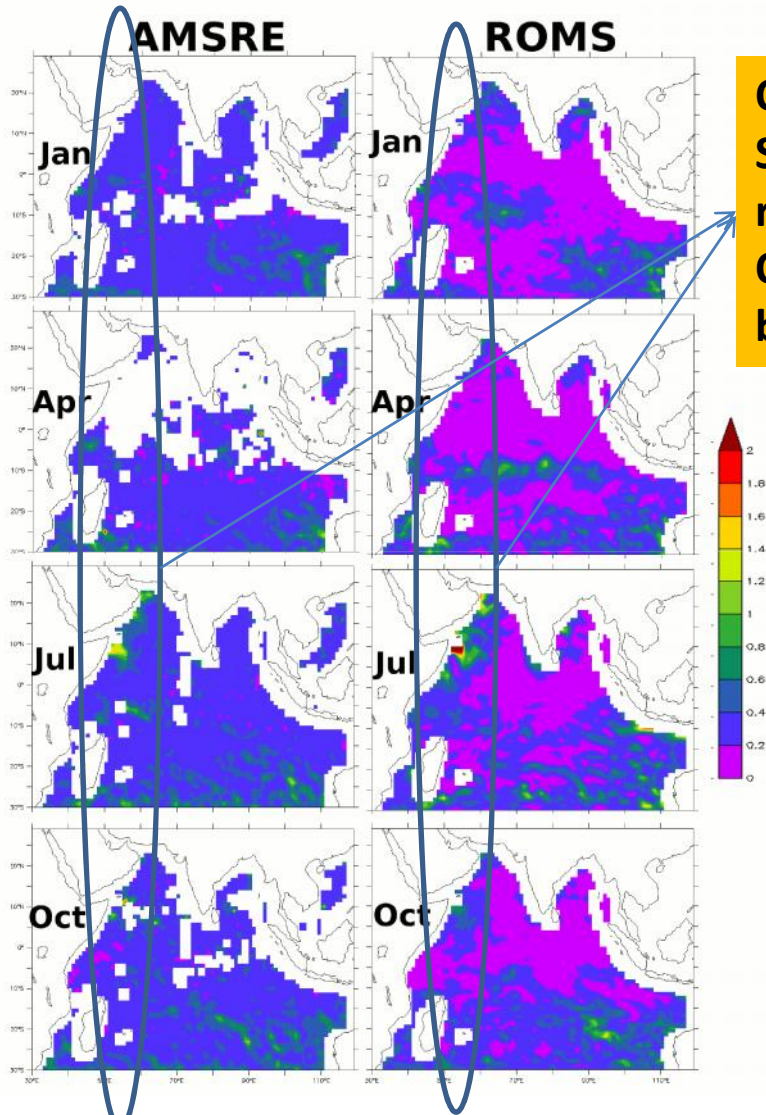


Structure and magnitudes of Estimated OEs are comparable to INCOIS-GODAS

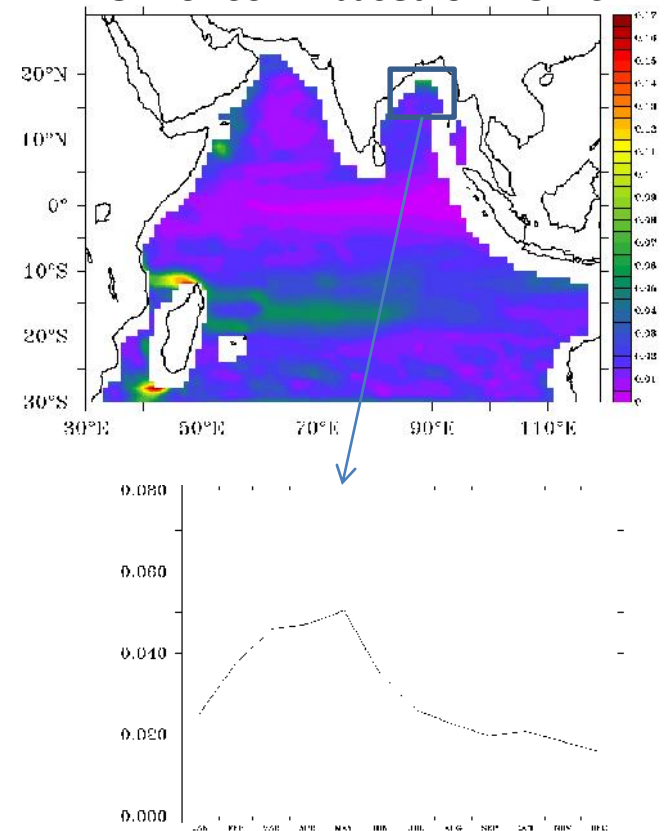


Observational Errors

OE for Sea Surface Temperature



OE for SSHA based on ROMS



Operational set up of INCOIS-GODAS

Model used : MOM 4
(GFDL)

Domain: Global

Resolution: 50 km zonal
and 25 km meridional,
40 vertical levels.

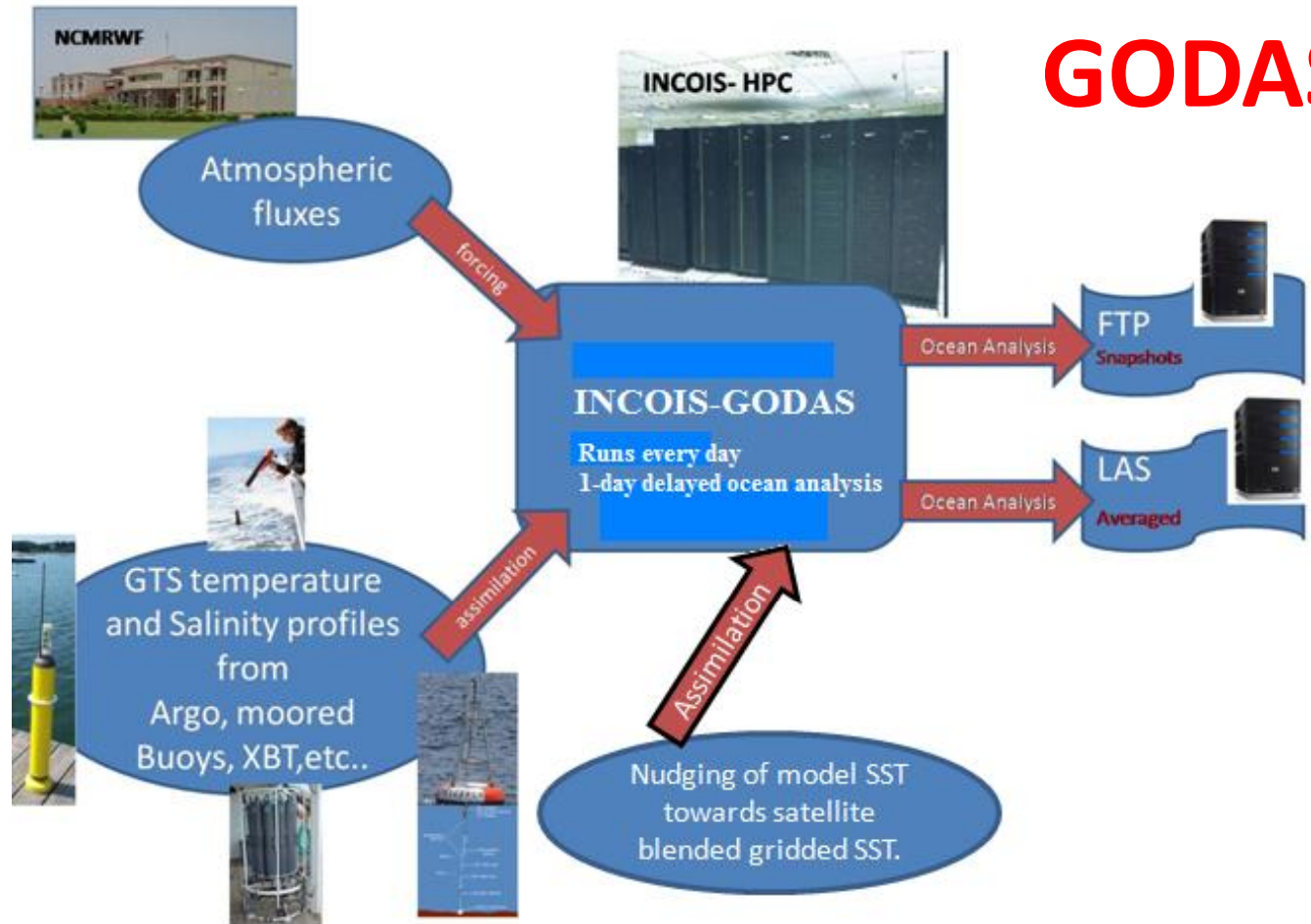
Atmospheric forcing:
Fluxes from Global
Assimilation Forecast
System (GFS)- T574L64
run at NCMRWF.

Data assimilation scheme:
3D VAR

Parameters assimilated:
Temperature and
salinity profiles from
Argo, moored
Buoys, XBT, etc...

Relaxation: OISST-V2
[Reynolds, 2007]

Outputs: Temperature,
Salinity, SSH, and
Currents



For more info: <http://www.incois.gov.in/portal/GODAS>

References:

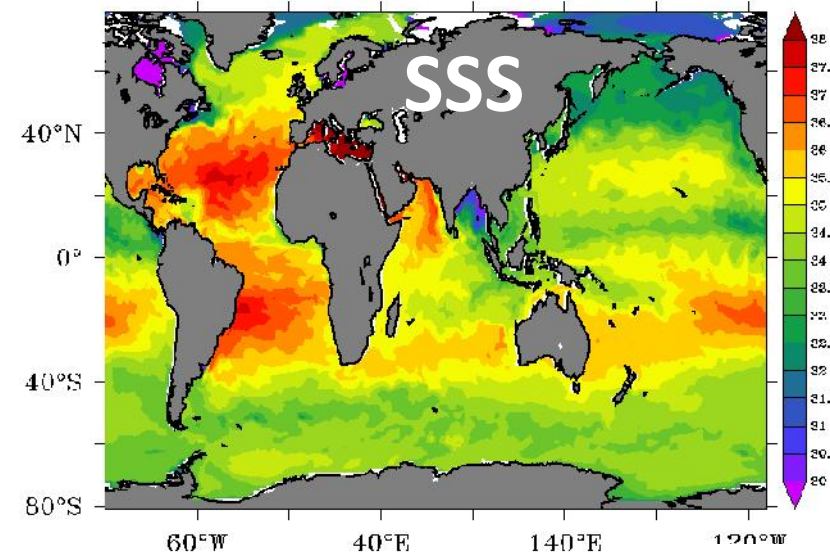
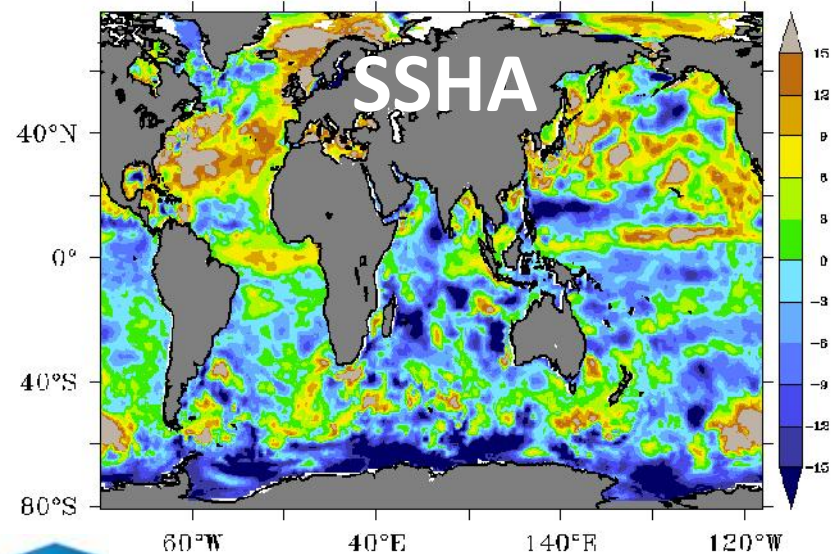
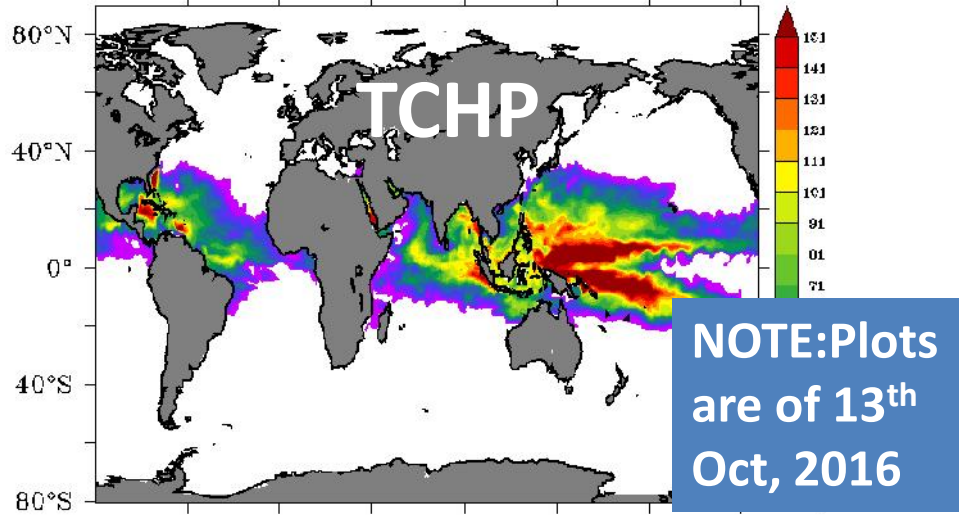
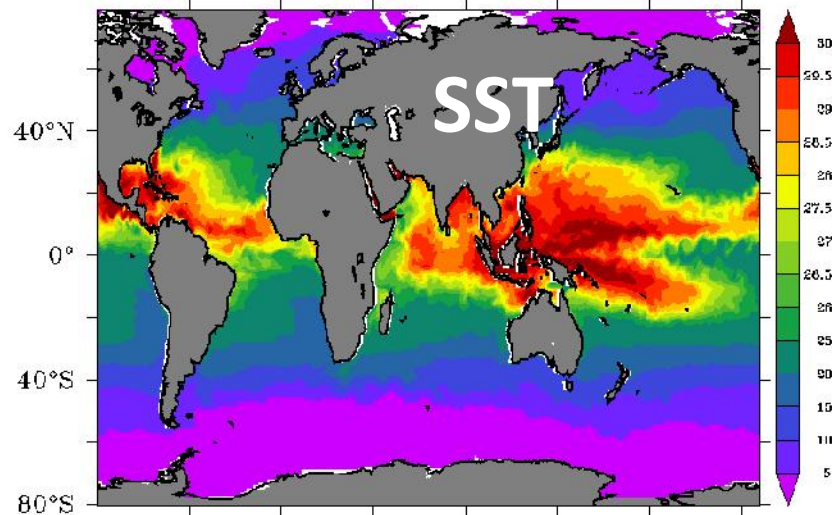
- 1) Ravichandran et al. , 2013, Ocean Modelling
- 2) Sivareddy et al., 2015, PhD thesis



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Real time (1-day delay) updates of the Global Ocean from INCOIS-GODAS: 2D fields

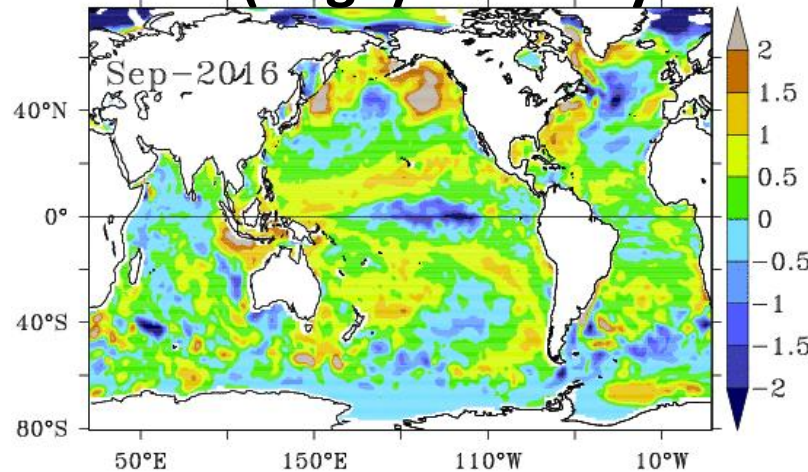


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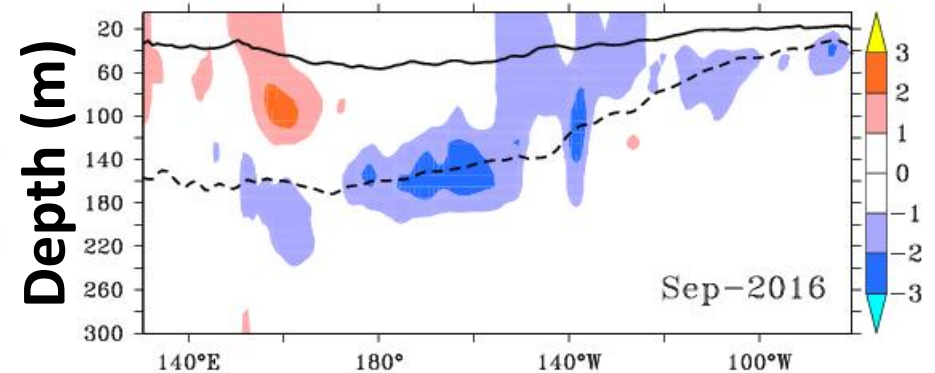


Climate Indices from INCOIS-GODAS

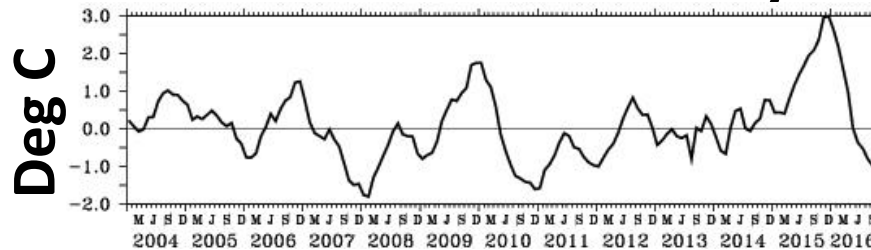
SST (degC) anomaly



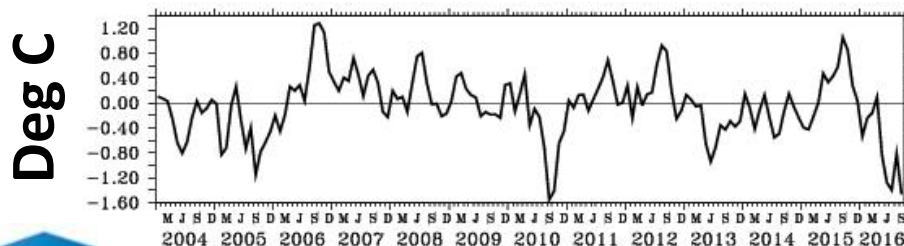
Temperature anomaly (deg C) averaged over 5S-5N latitudes



NiNO 3.4 SST anomaly



IOD index



Monthly updates of climate indices are available by 10th of each month.

Service is started in April, 2014.

The information is being disseminated from the INCOIS web site

www.incois.gov.in/portal/ElNino



Users of INCOIS-GODAS analysis

- Analysis are used as initial and boundary conditions to operational ROMS at INCOIS
- Ocean initial conditions are provided to IITM, Pune for CFS-V2
- Global maps of SST and SST anomalies are provided to IMD-Pune
- Climate indices are used in MoES-ENSO bulletins
- Researchers across globe



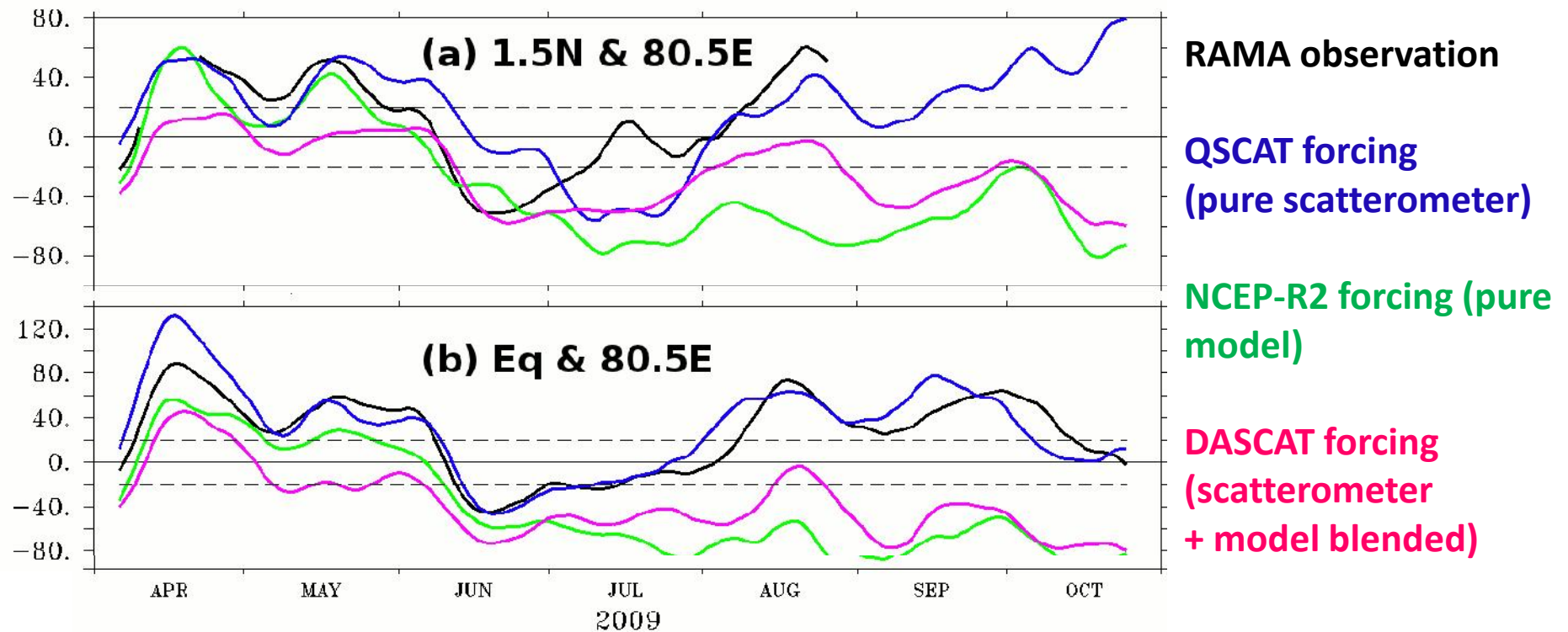
Ocean Re-analysis from INCOIS-GODAS

- Forcing
 - Improved atmospheric forcing from NCMRWF GFS-T574L64 that is available at 4 times daily temporal and 0.25 x 0.25 spatial resolutions
 - Improved wind forcing from scatterometers
 - Inter-annual monthly river discharge to improve seasonal cycles in the Head BoB.
- Assimilation
 - Assimilates delayed mode temperature and salinity profiles only from Argo and ship-based networks to avoid spurious assimilation shocks from moored buoys.
 - Relaxes model SST towards Reynolds SST
- Outputs
 - 3D fields of T, S, zonal and meridional currents, vertical velocity
 - 2D fields of SSHA and MLD
 - Available at 4 times daily resolution



Wind forcing from pure scatterometer winds improves ocean model simulations

Zonal surface currents (cm/s) from RAMA observation and INCOIS-GODAS simulations



Sivareddy et al., 2015. Assessing the impact of various wind forcing on INCOIS-GODAS simulated ocean currents in the equatorial Indian Ocean. *Ocean Dynamics*, 65 (9-10), pp. 1235-1247.

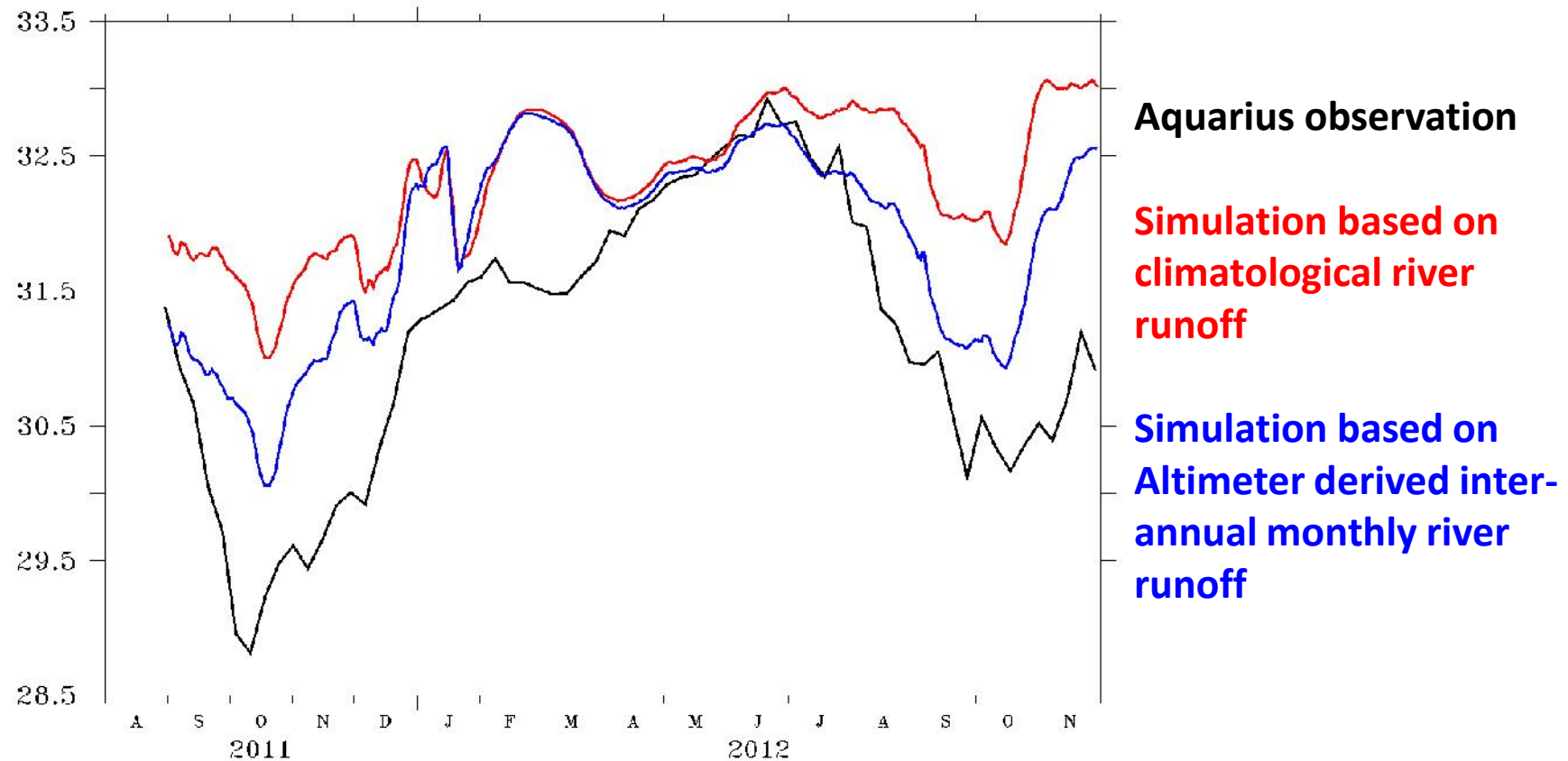


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River runoff estimated from altimeter measurements improves salinity simulations in INCOIS-GODAS

Sea surface salinity averaged over north BoB



Sivareddy, S., 2015. A study on global ocean analysis from an ocean data assimilation system and its sensitivity to observations and forcing fields, Ph.D. thesis, Andhra University.

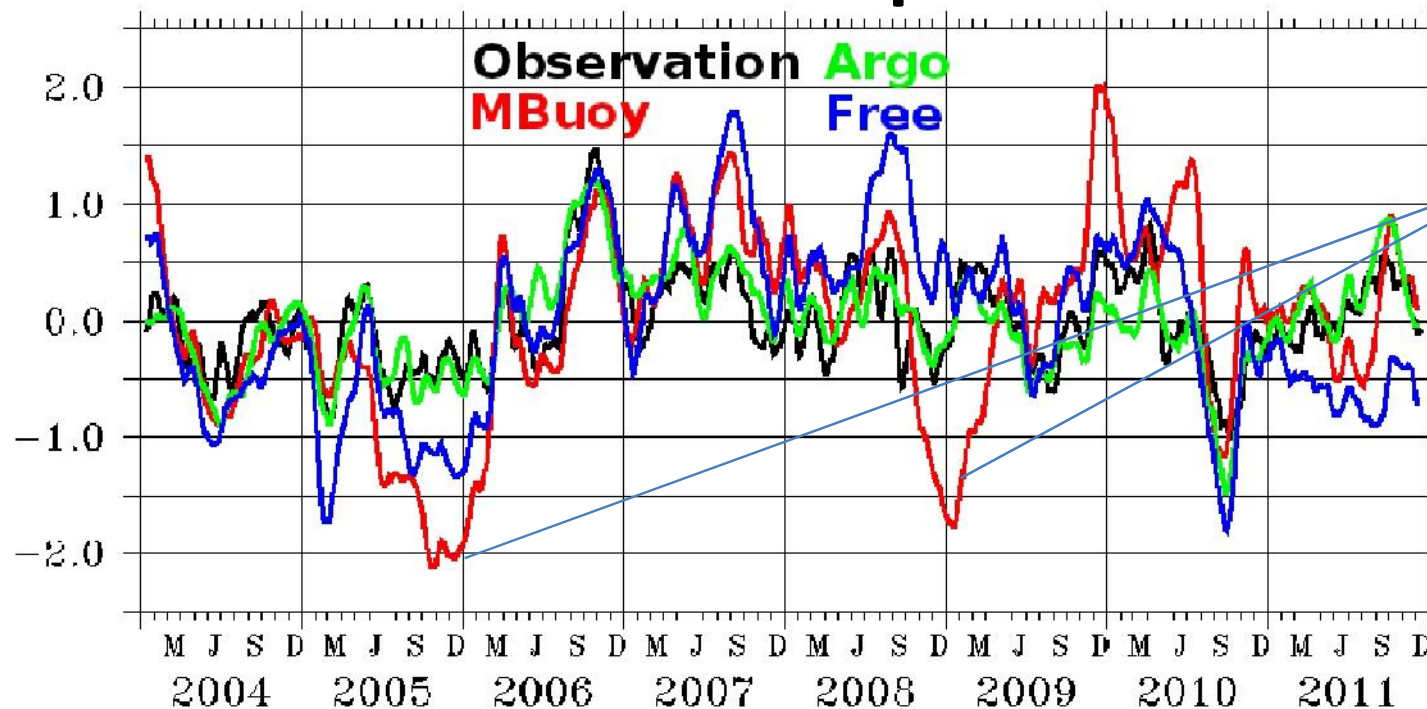


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Tropical Mbuoy observations causes spurious assimilation shocks: Demonstration

Indian Ocean Dipole index

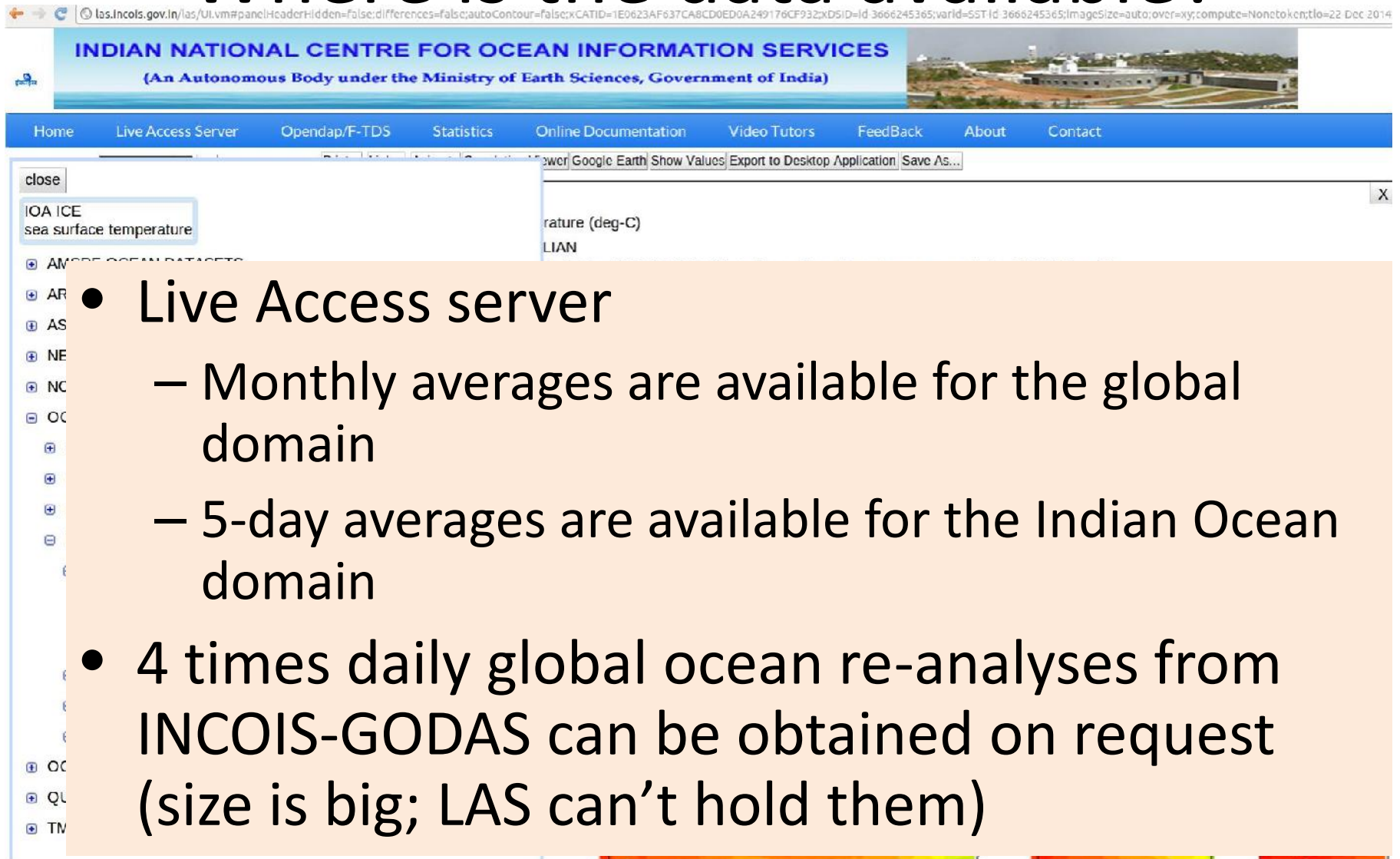


Mbuoy exp
Wrongly
interpreted
neutral IOD as
strong -ve IOD
years.
Importantly,
the simulation
is worse than
Free exp.

S. Sivareddy, Arya Paul, Travis Sluka, M Ravichandran and Eugenia Kalnay (2017), The pre-argo ocean reanalysis may be seriously affected by the spatial coverage of moored-buoys, under revision in Nature Scientific Reports.



Where is the data available?



The screenshot shows the INCOIS website interface. The header includes the INCOIS logo and the text "INDIAN NATIONAL CENTRE FOR OCEAN INFORMATION SERVICES (An Autonomous Body under the Ministry of Earth Sciences, Government of India)". The navigation bar contains links: Home, Live Access Server, Opendap/F-TDS, Statistics, Online Documentation, Video Tutors, FeedBack, About, and Contact. The main content area displays a "Live Access Server" window with a search bar containing "IOA ICE sea surface temperature". A dropdown menu shows "rature (deg-C)" and "LIAN". A list of datasets is visible on the left, including "AMODE OCEAN DATASETS", "AR", "AS", "NE", "NC", "OC", "OC", "QU", and "TM".

- Live Access server
 - Monthly averages are available for the global domain
 - 5-day averages are available for the Indian Ocean domain
- 4 times daily global ocean re-analyses from INCOIS-GODAS can be obtained on request (size is big; LAS can't hold them)



Thank You



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Theme: Model validation

Estimated parameters

- Mixed layer Depth
 - Definition: Mixed-layer is the layer between the ocean surface and a depth usually ranging *between 25 and 200m*, where the density is about the same as at the surface. The mixed-layer owes its existence to the mixing initiated by waves and turbulence caused by the wind stress on the sea surface.
 - MLD is estimated based on the method suggested by Sprintall and Tomczak, 1992 by setting ΔT to 0.8.
- Depth of 20 degree isotherm
 - The depth of 20°C isotherm from the surface is broadly used as the thermocline depth for tropical ocean studies (Meyers 1979; Kessler 1990; Vialard and Delecluse 1998; Durand and Delcroix 2000; Meinen and McPhaden 2000; Fedorov and Philander 2001; Chepurin et al. 2005; Sourav and Arun, 2012) because the 20°C isotherm is located near the center of the main thermocline.
 - The mechanism of variation 20°C isotherm depth (D20) is important to study as it indicates the oceanic upwelling and downwelling processes and indicates the thermocline variability of the ocean (Haijun and Wang 2008). Braganza (2008) and Rao and Behera (2005) explain that there are cases where changes in the thermocline depth may act as a precursor to subsequent changes at the surface during strong upwelling, and this will cause potential cooling of the surface temperature. During the case when upwelling is not strong enough to influence the surface, it acts upon the bottom of the mixed layer.

Statistical parameters

$$\overline{X} = \frac{1}{n} \sum_{i=1}^n X_i$$

$$Bias = \overline{X} - \overline{Y}$$

$$\dagger_X = \sqrt{\frac{1}{n} \sum_{i=1}^n (X_i - \overline{X})^2}$$

$$RMSD = \sqrt{\frac{1}{n} \sum_{i=1}^n (X_i - Y_i)^2}$$

$$Correl = \frac{\sum_{i=1}^n (X_i - \overline{X})(Y_i - \overline{Y})}{(n-1)\dagger_X \dagger_Y}$$

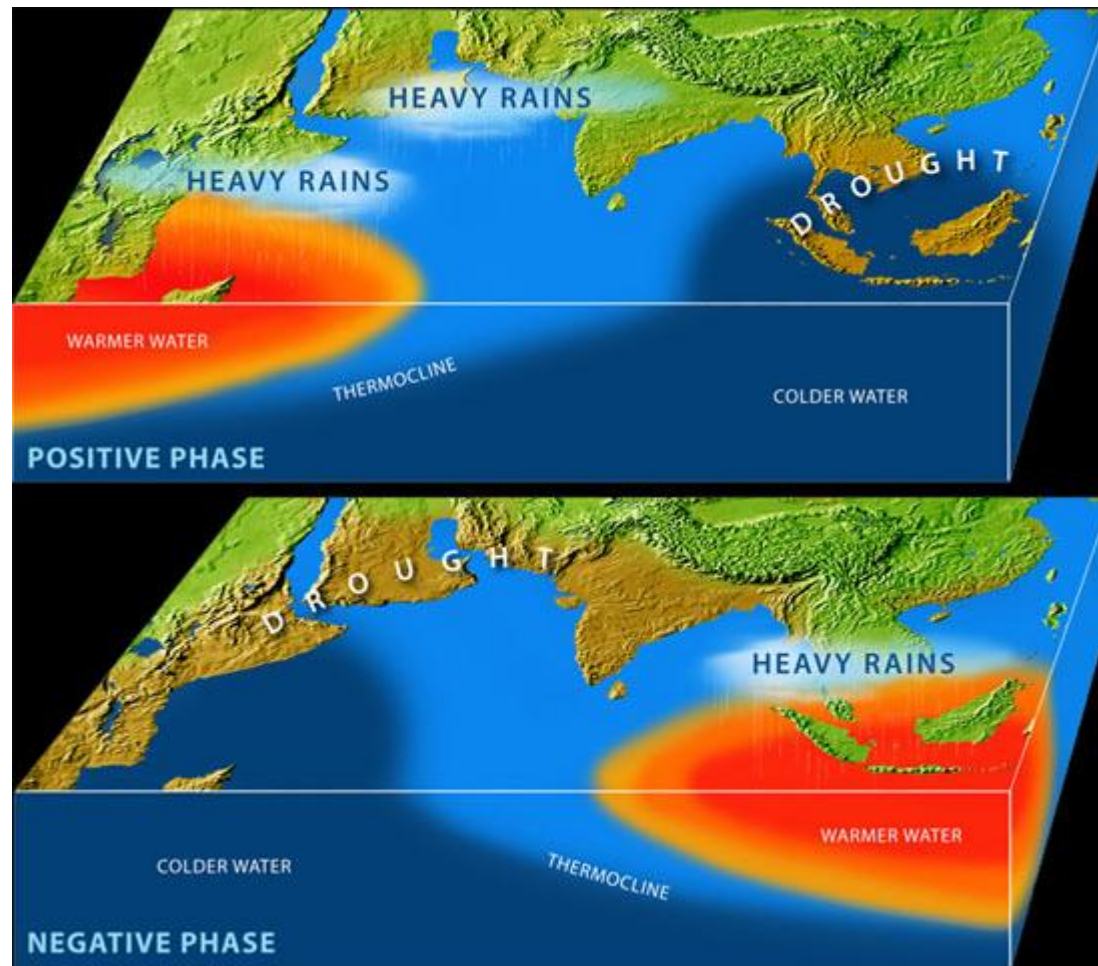
Data Sets

- Time series measurements from RAMA buoy network
 - Temperature
 - Daily averages
 - Available at depths 1.5, 5, 15, 25, 50, 75, 100, 125, 150, 200, 250, 300, 500, 750 m
 - Currents
 - Daily averages
 - Available at 10m depth
 - Source: www.pmel.noaa.gov/tao
 - Reference: McPhaden et al. (2009b)
- REYNOLDS SST:
 - Satellite and in-situ blended level-4 gridded SST product
 - Daily averages at 0.25 X 0.25
 - Source: <ftp.emc.ncep.noaa.gov>
 - Reference: Reynolds et al. (2007)
- OSCAR:
 - Ocean Surface currents (0-30m average) derived from satellite measurements of winds, SSHA and SST
 - 5-day averages at 1/3 X 1/3
 - Source: www.oscar.noaa.gov
 - Reference: Bonjean and Lagerloef (2002)

Theme: Climate Indices

Indian Ocean Dipole

The Indian Ocean Dipole (IOD) is defined by the difference in sea surface temperature between two areas (or poles, hence a dipole) – a western pole in the Arabian Sea (western Indian Ocean) and an eastern pole in the eastern Indian Ocean south of Indonesia. The IOD affects the climate of India and other countries that surround the Indian Ocean Basin, and is a significant contributor to rainfall variability in this region.

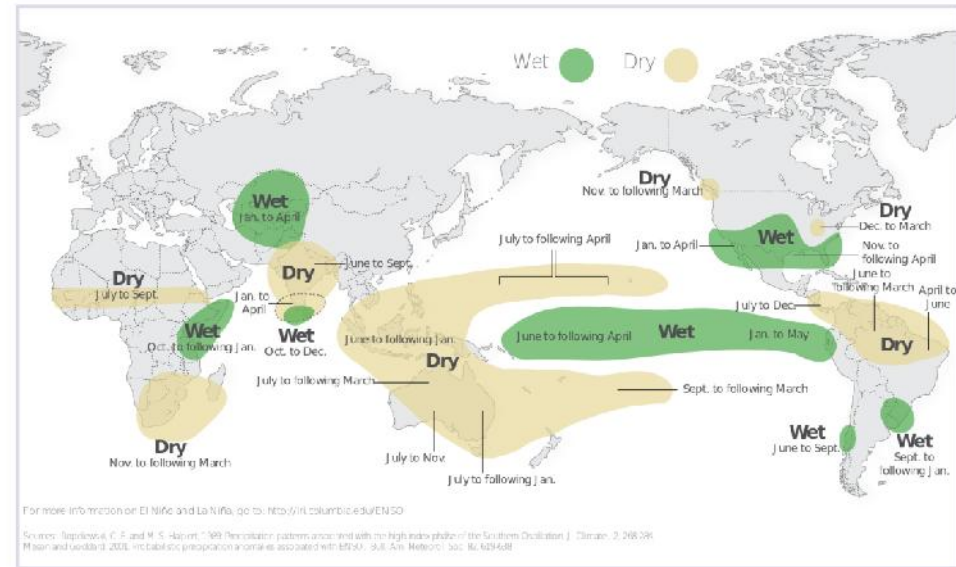


Source: www.meted.ucar.edu

El Niño

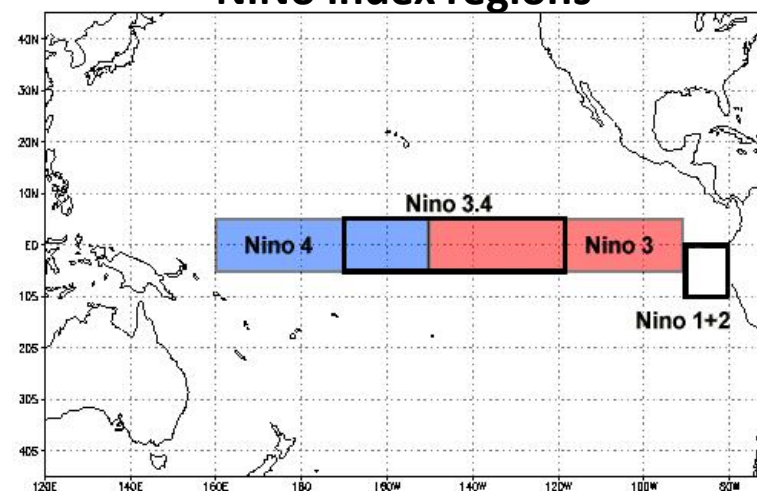
El Niño and Rainfall

El Niño conditions in the tropical Pacific are known to shift rainfall patterns in many different parts of the world. Although they vary somewhat from one El Niño to the next, the strongest shifts remain fairly consistent in the regions and seasons shown on the map below.

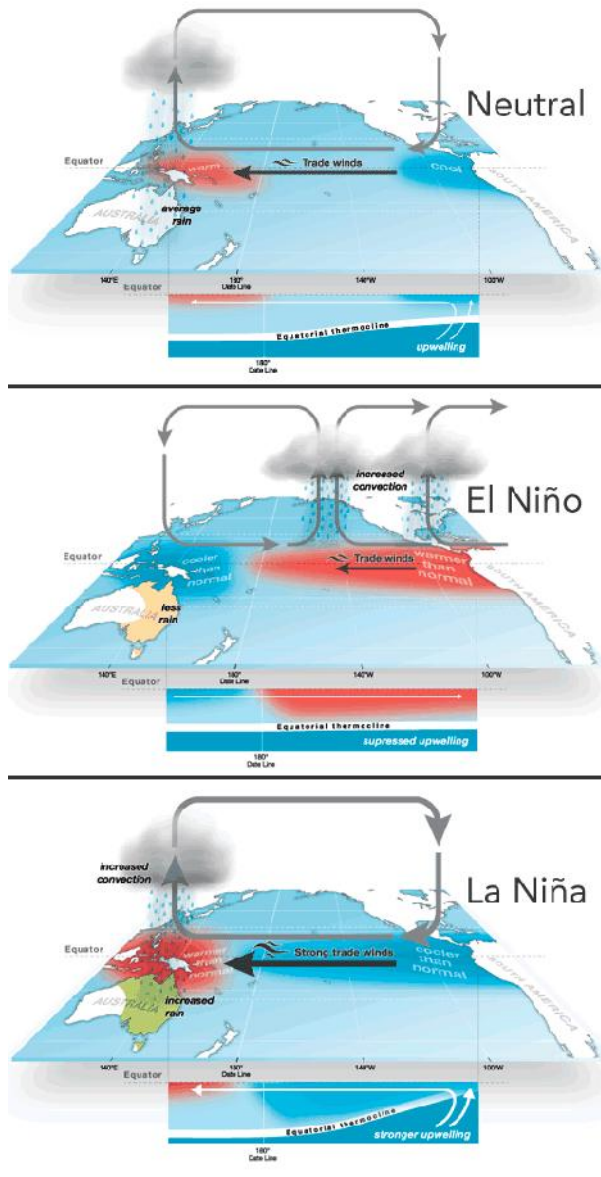


Source: www.climate.gov

NiNo index regions



Source: www.ncdc.noaa.gov



Images from the [Australian Bureau of Meteorology](http://www.bom.gov.au).